



1.2.3 Einige Rechenregeln

Sinus

$$\sin(2\pi \cdot n + \alpha) = \sin(\alpha)$$

$$\sin(-\alpha) = -\sin(\alpha)$$

$$\sin\left(\frac{\pi}{2} \pm \alpha\right) = \cos(\alpha)$$

$$\sin(\pi \pm \alpha) = \mp \sin(\alpha)$$

$$\sin\left(\frac{3\pi}{2} \pm \alpha\right) = -\cos(\alpha)$$

$$\sin(2\pi - \alpha) = -\sin(\alpha)$$

Kosinus

$$\cos(2\pi \cdot n + \alpha) = \cos(\alpha)$$

$$\cos(-\alpha) = \cos(\alpha)$$

$$\cos\left(\frac{\pi}{2} \pm \alpha\right) = \mp \sin(\alpha)$$

$$\cos(\pi \pm \alpha) = -\cos(\alpha)$$

$$\cos\left(\frac{3\pi}{2} \pm \alpha\right) = \pm \sin(\alpha)$$

$$\cos(2\pi - \alpha) = \cos(\alpha)$$

Sinus und Kosinus

$$\sin(\alpha)^2 + \cos(\alpha)^2 = 1$$

(Pythagoras am Einheitskreis)

$$\sin(\alpha \pm \beta) = \sin(\alpha)\cos(\beta) \pm \cos(\alpha)\sin(\beta)$$

(Additionstheoreme)

Wichtige Winkel

$$\sin(0) = \sin(0^\circ) = 0 = \cos(90^\circ) = \cos\left(\frac{\pi}{2}\right) = \frac{1}{2}\sqrt{0}$$

$$\sin\left(\frac{\pi}{6}\right) = \sin(30^\circ) = \frac{1}{2} = \cos(60^\circ) = \cos\left(\frac{\pi}{3}\right) = \frac{1}{2}\sqrt{1}$$

$$\sin\left(\frac{\pi}{4}\right) = \sin(45^\circ) = \frac{1}{2}\sqrt{2} = \cos(45^\circ) = \cos\left(\frac{\pi}{4}\right) = \frac{1}{2}\sqrt{2}$$

$$\sin\left(\frac{\pi}{3}\right) = \sin(60^\circ) = \frac{1}{2}\sqrt{3} = \cos(30^\circ) = \cos\left(\frac{\pi}{6}\right) = \frac{1}{2}\sqrt{3}$$

$$\sin\left(\frac{\pi}{2}\right) = \sin(90^\circ) = 1 = \cos(0^\circ) = \cos(0) = \frac{1}{2}\sqrt{4}$$